

# Turn on the super-elastic collision nature of CMEs through low approaching speed

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# Type of collision nature

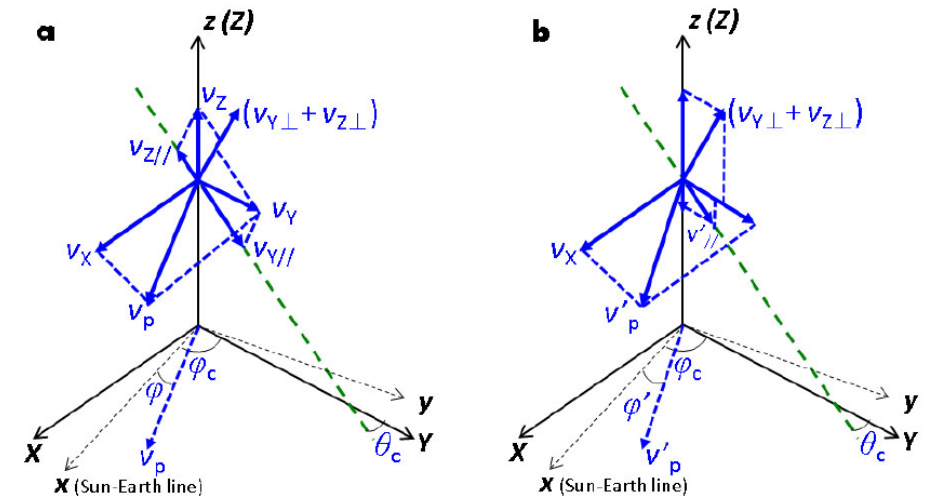
Type	$e$	Total kinetic energy
Merging	$-1 < e < 0$	Decrease
Perfectly inelastic	$e = 0$	Decrease
Inelastic	$0 < e < 1$	Decrease
Elastic	$e = 1$	Conserved
Super-elastic	$ e  > 1$	Increase

Two measures

- Coefficient of restitution

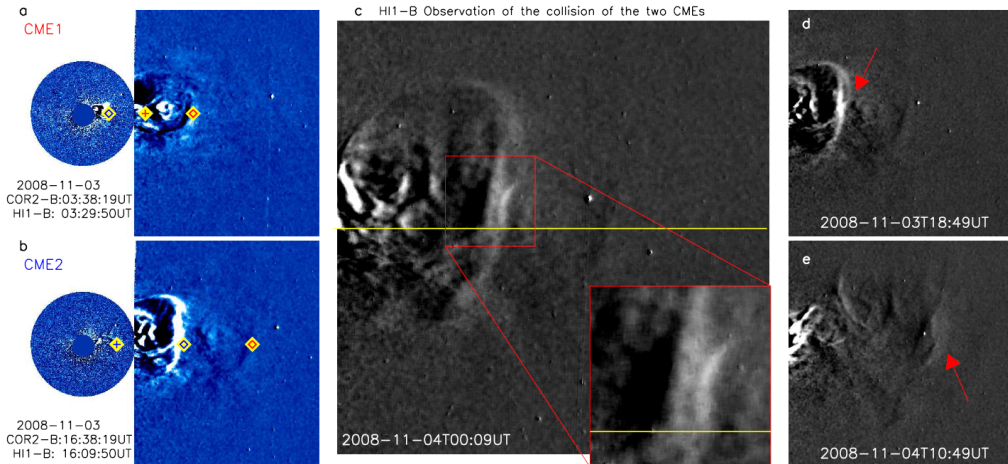
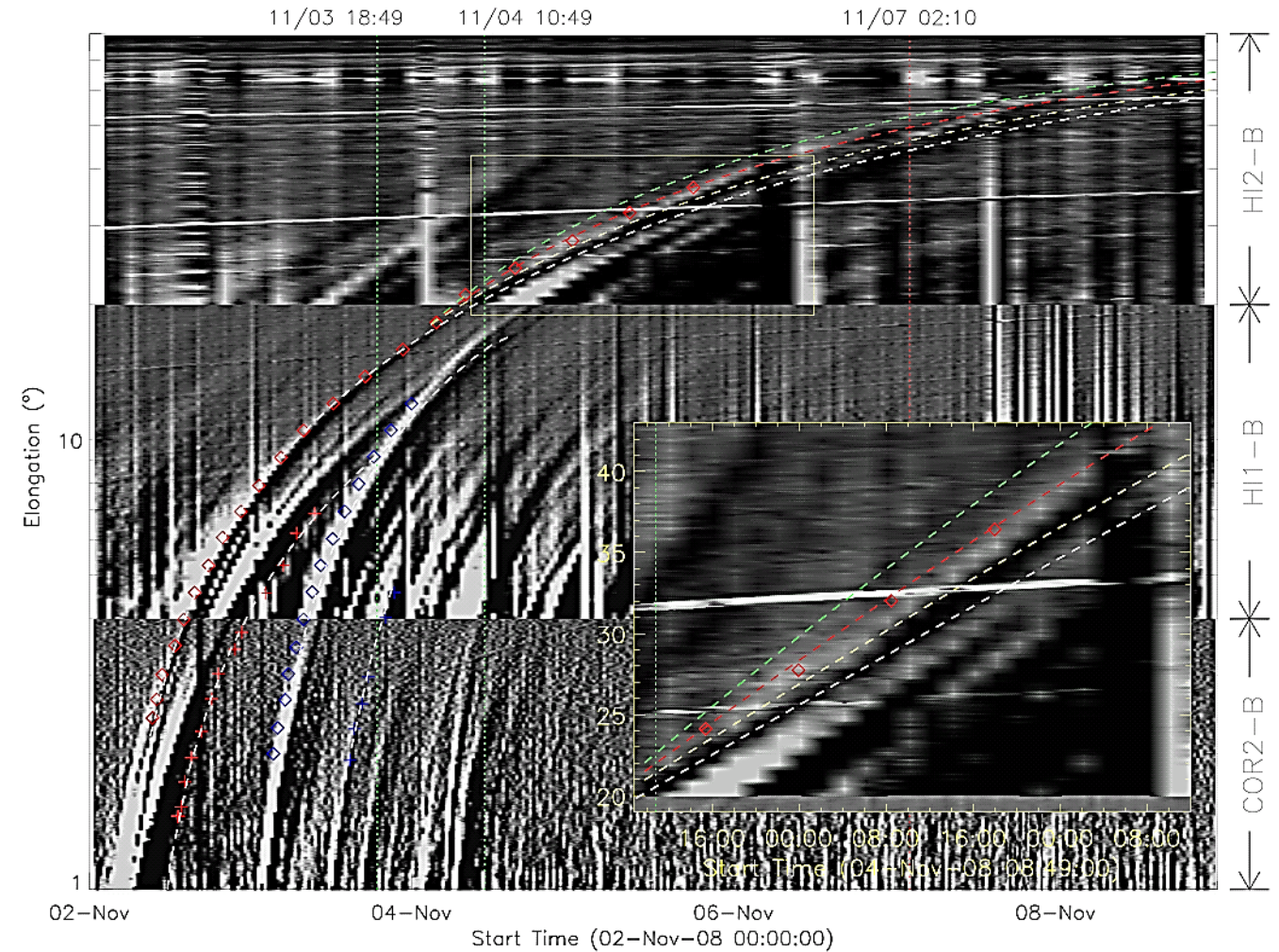
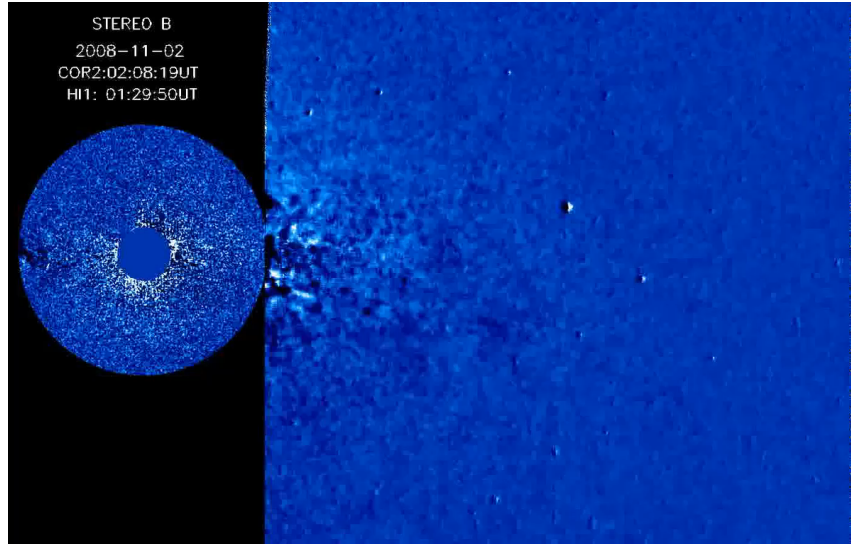
$$e = (v'_2 - v'_1) / (v_1 - v_2)$$

- Total kinetic energy



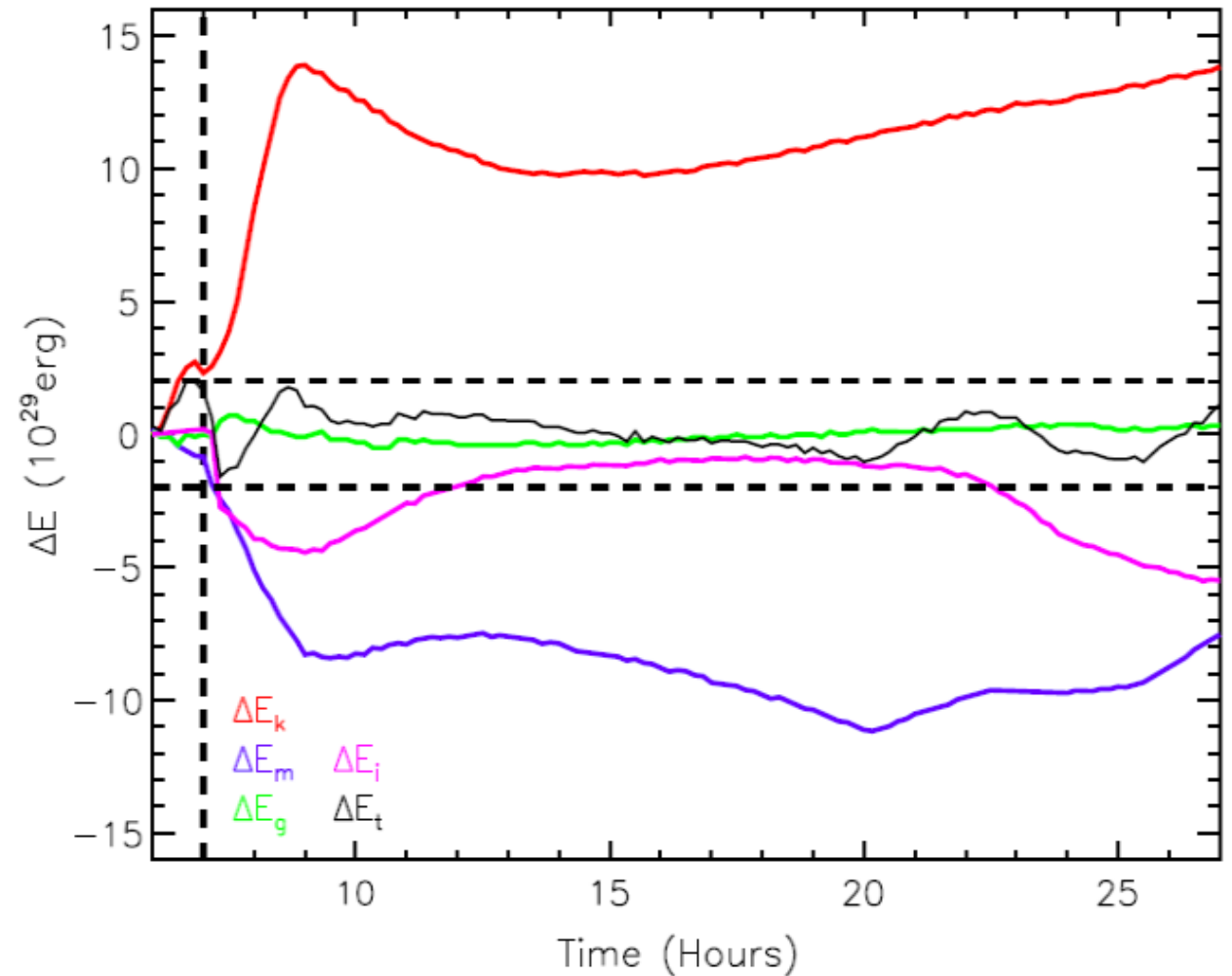
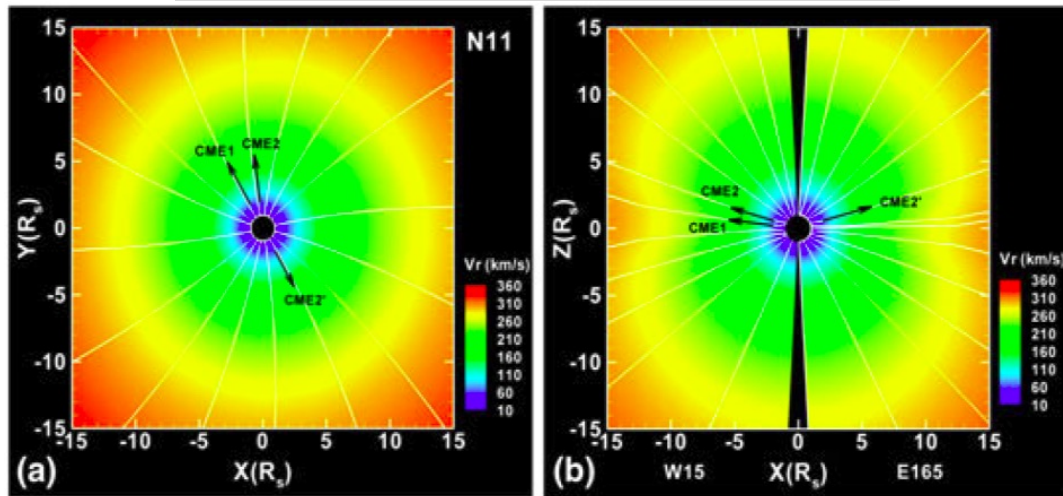
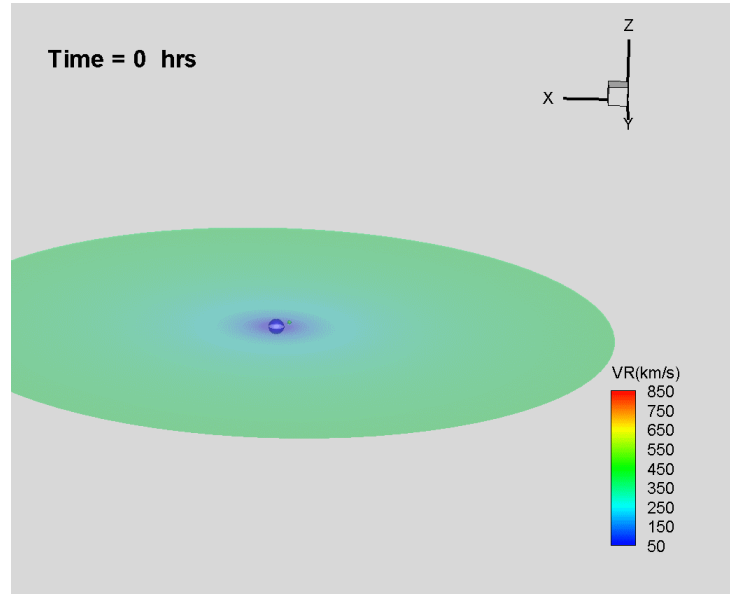
# Propose the possibility of super-elastic collision between CMEs

(Shen C., et al., Nat. Phys., 2012)



# Verified with 3D MHD numerical simulations

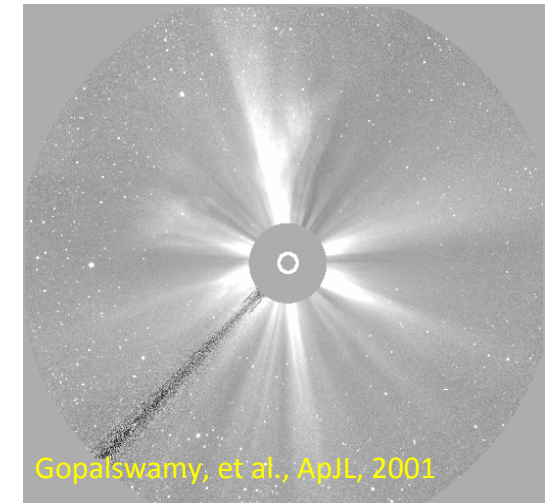
(Shen F., et al., GRL, 2013)



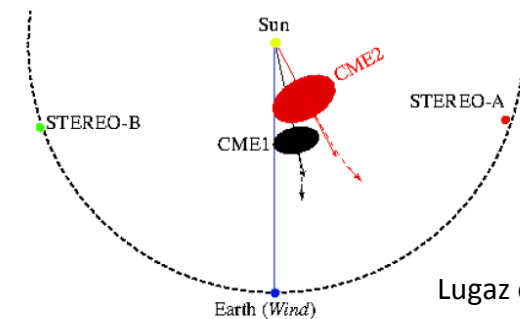
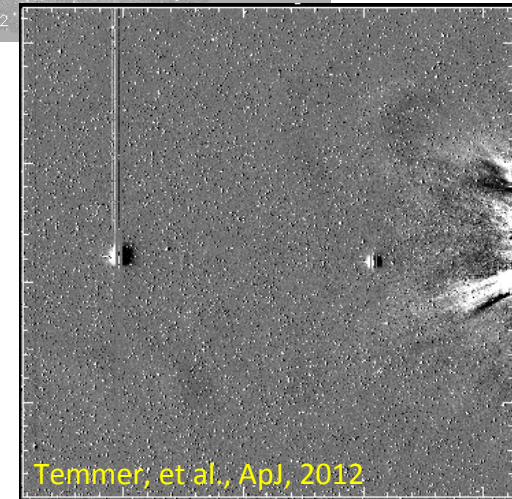
## However .....

- Gopalswamy et al., 2001, ApJL: Cannibalism of two CMEs --- **merging?**
- Lugaz et al., 2009, AG:  $V_{cme1}$ : 600  $\rightarrow$  850 – 900 km/s,  $V_{cme2}$ : 1200 – 1300  $\rightarrow$  800 km/s --- possibilities of **perfectly inelastic**, **elastic** and **shock effect** were discussed
- Temmer et al., 2012, ApJ: before collision,  $V_{cme1} \sim 600$  km/s and  $V_{cme2} \sim 1400$  km/s; after collision, merged feature  $\sim 800$  km/s --- **“super” inelastic**  $\rightarrow$  **merging?**
- Lugaz et al., 2012, ApJ:  $V_{cme1}$  increases a little,  $V_{cme2}$ : 600  $\rightarrow$  380 km/s --- **perfectly inelastic**
- Lugaz et al., 2013, ApJ: Simulation Case B, minimum reconnection;  $V_{cme1}$ : 600  $\rightarrow$  650 km/s,  $V_{cme2}$ : 1000  $\rightarrow$  650 km/s --- **“super” inelastic**  $\rightarrow$  **merging?**
- Temmer et al., 2014, ApJ:  $V_{cme1}$ : 400  $\rightarrow$  700 km/s  $V_{cme2}$ : 1300  $\rightarrow$  600 km/s --- **“super” inelastic**  $\rightarrow$  **merging?**
- Mishra et al., 2015, SoPh:  $V_{cme1}$ : 365  $\rightarrow$  450 km/s,  $V_{cme2}$ : 625  $\rightarrow$  430 km/s --- **inelastic**
- Colaninno & Vourlidas, 2015: **super-elastic**
- Shen et al., 2012, NP:  $V_{cme1}$ : 240  $\rightarrow$  320 km/s,  $V_{cme2}$ : 410  $\rightarrow$  350 km/s --- **super-elastic**

Approaching speed might play an important role



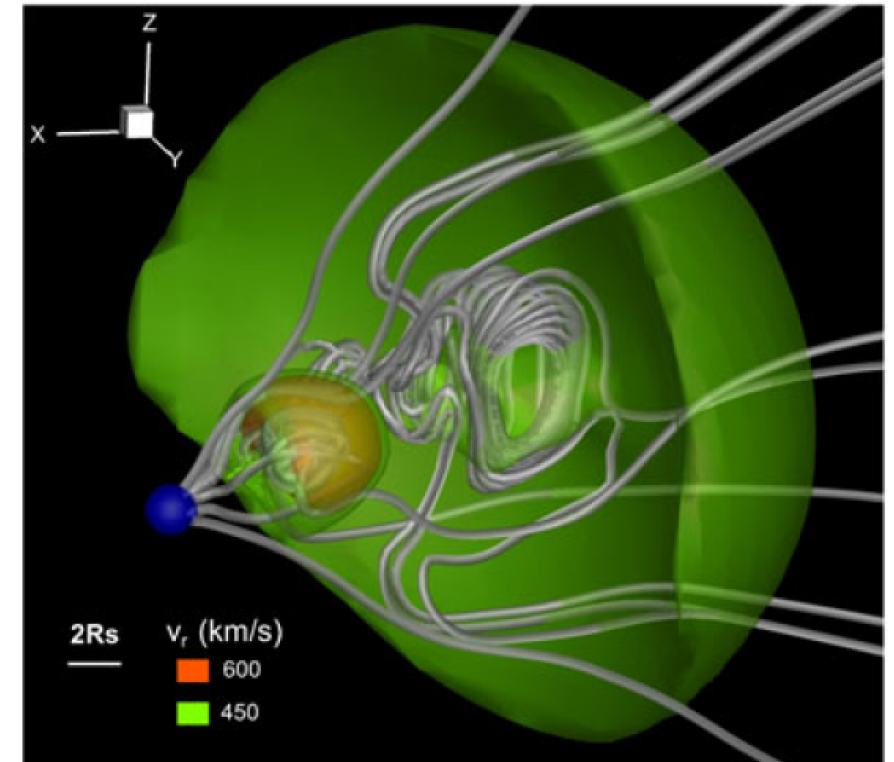
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Lugaz et al., ApJ, 2012

# Numerical experiments

- MHD Model
  - 3-D corona-interplanetary total variation diminishing (COIN- TVD) scheme in a Sun-centered spherical coordinate system
  - Non-reflecting Boundary Conditions at lower boundary
- CME Initiation
  - A high-density, -velocity, -temperature, and magnetized plasma blob is superposed on the background solar wind model

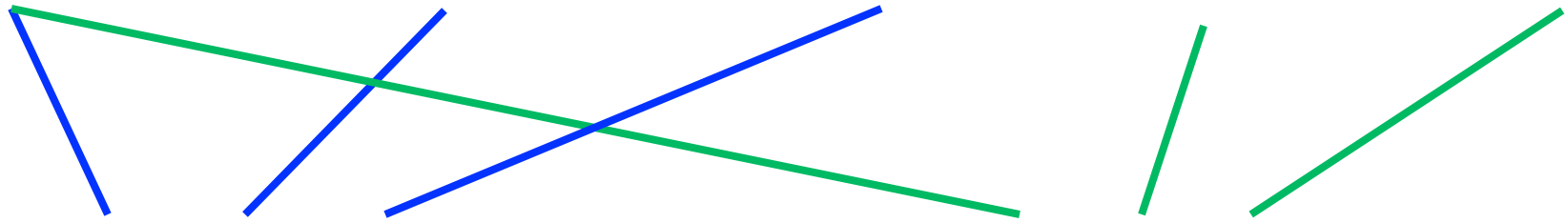


## Five test cases --- Setup

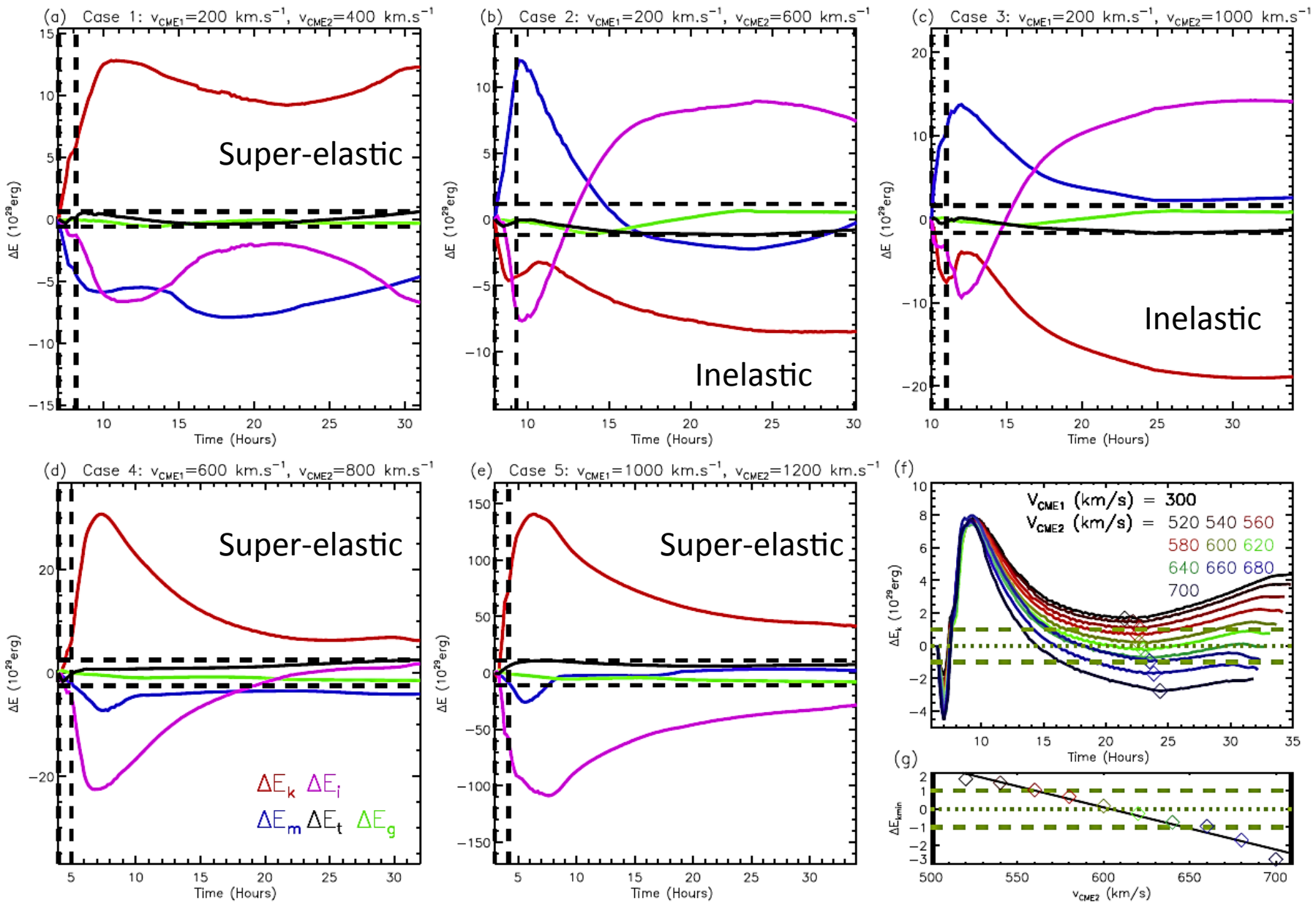
Common par.	Direction	$R$	$B$	$n$	$T$	$E_m$	$E_i$	$E_g$	$V_{sw}$	
		$R_s$	$\times 10^5$ nT	$\times 10^7$ cm $^{-3}$	$\times 10^5$ K	$\times 10^{31}$ erg			km s $^{-1}$	
	N11W18	0.5	1.47	4.0	5.0	1.50	1.37	-0.64	316 ~ 461	
Other par.	Case 1		Case 2		Case 3		Case 4		Case 5	
	CME1	CME2	CME1	CME2	CME1	CME2	CME1	CME2	CME1	CME2
$V_{CME}$ (km s $^{-1}$ )	200	400	200	600	200	1000	600	800	1000	1200
$E_k$ ( $\times 10^{31}$ erg)	0.513	1.83	0.513	3.44	0.513	9.13	3.44	5.96	9.13	12.9
$E_t$ ( $\times 10^{31}$ erg)	2.74	4.06	2.74	5.67	2.74	11.36	5.67	8.19	11.36	15.13
$t_s$ (hours)	7		8		10		4		3	

Same  $V_{cme1}$ , different  $\Delta V$

Different  $V_{cme1}$ , same  $\Delta V$

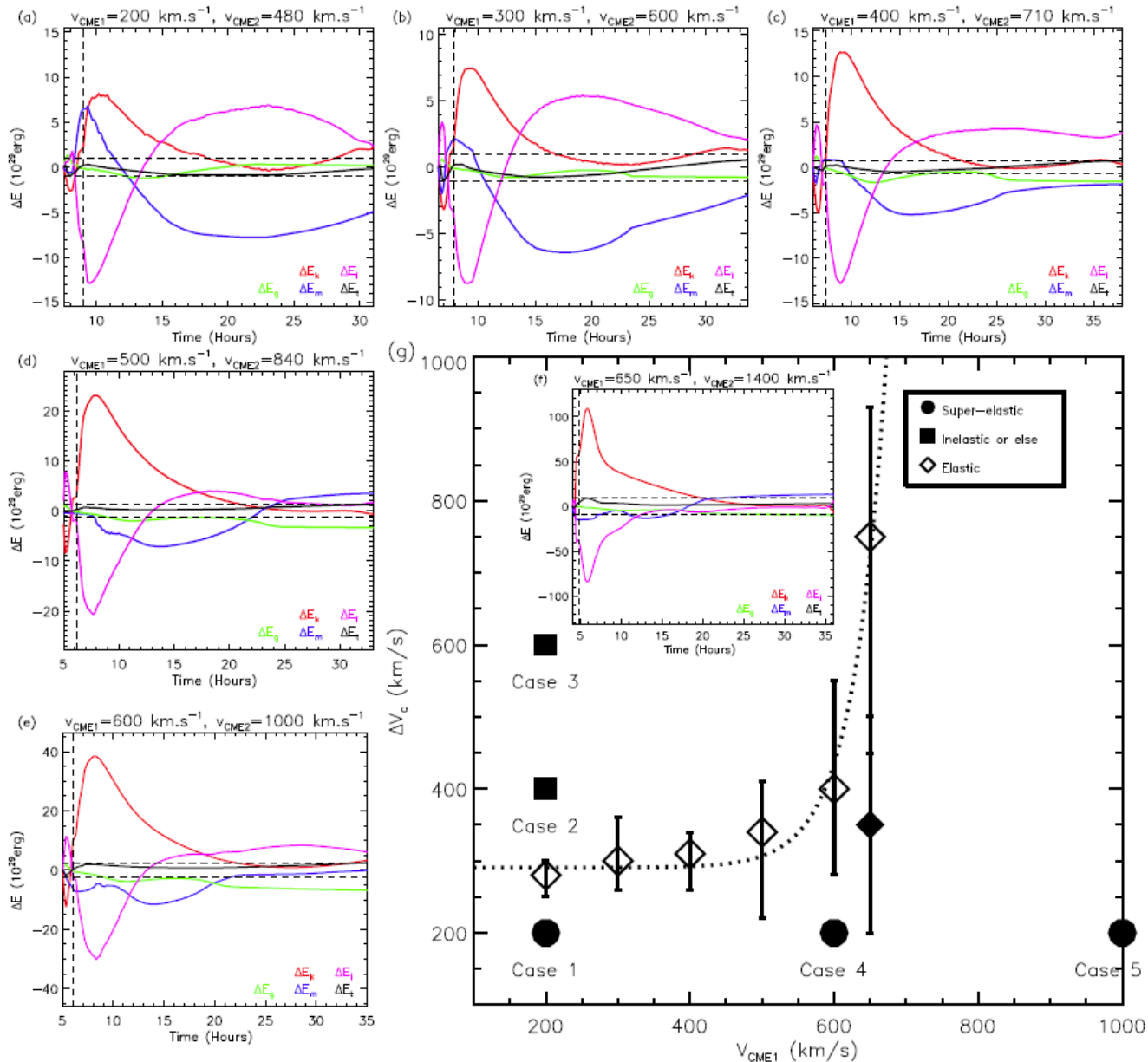


# Five test cases --- Results





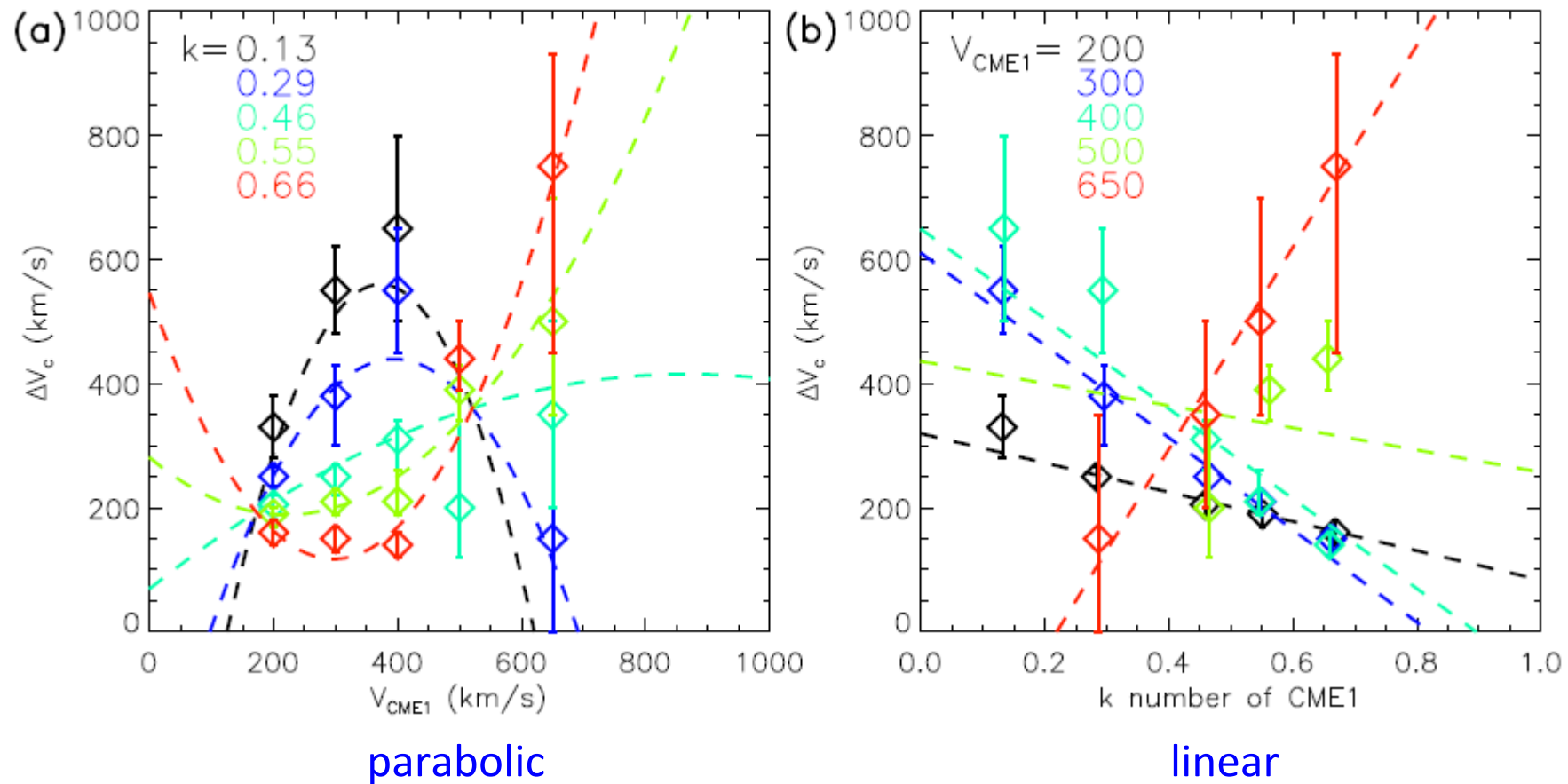
# Search the boundary between the super-elastic and inelastic nature



Critical value of the approaching speed  $\Delta V$

- Dependent on CME speed, e.g.,  $v_{cme1}$
- Dependent on the ratio of CME kinetic energy to the total energy, defined as k-number
  - ✓  $k > 0.5$  means kinetic energy is dominant, otherwise kinetic energy is a minor one.

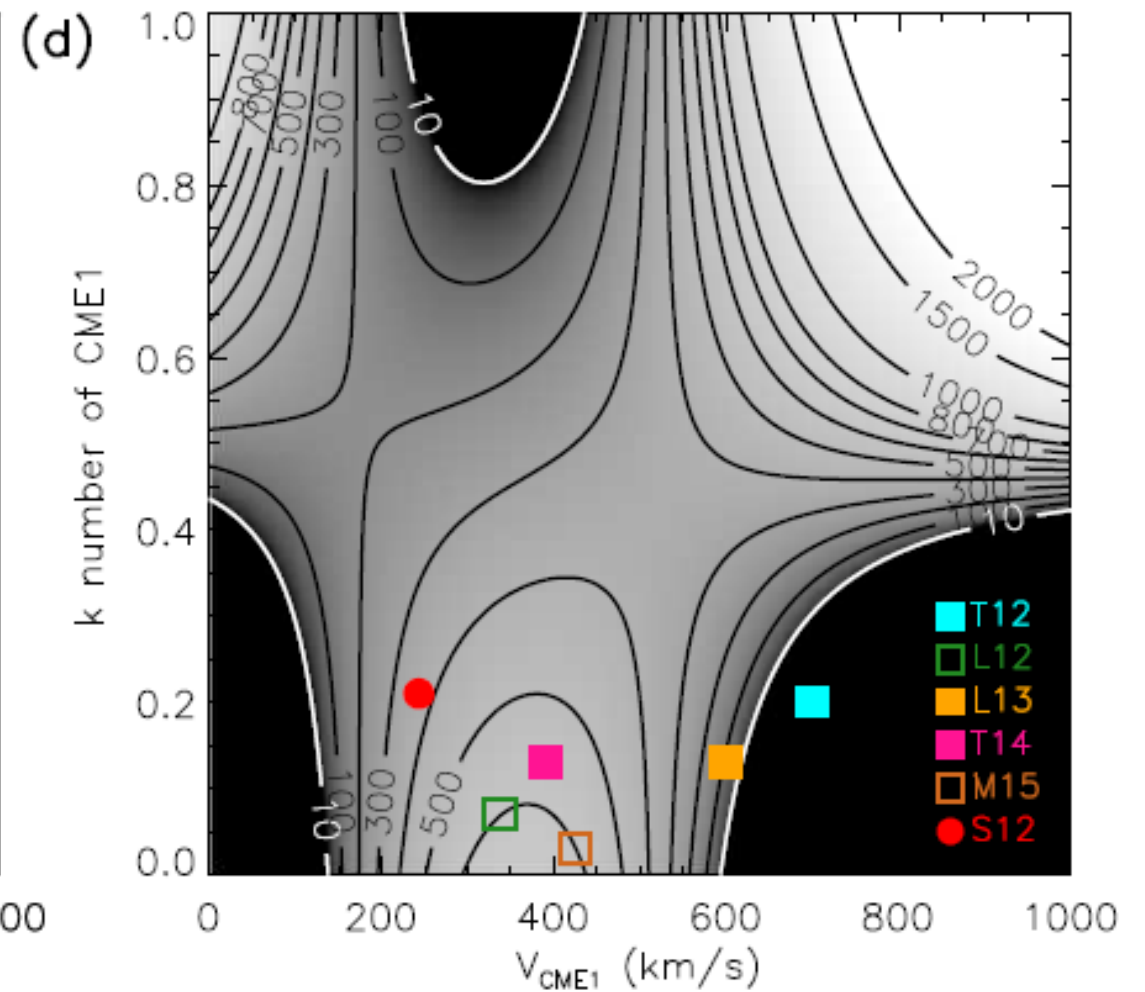
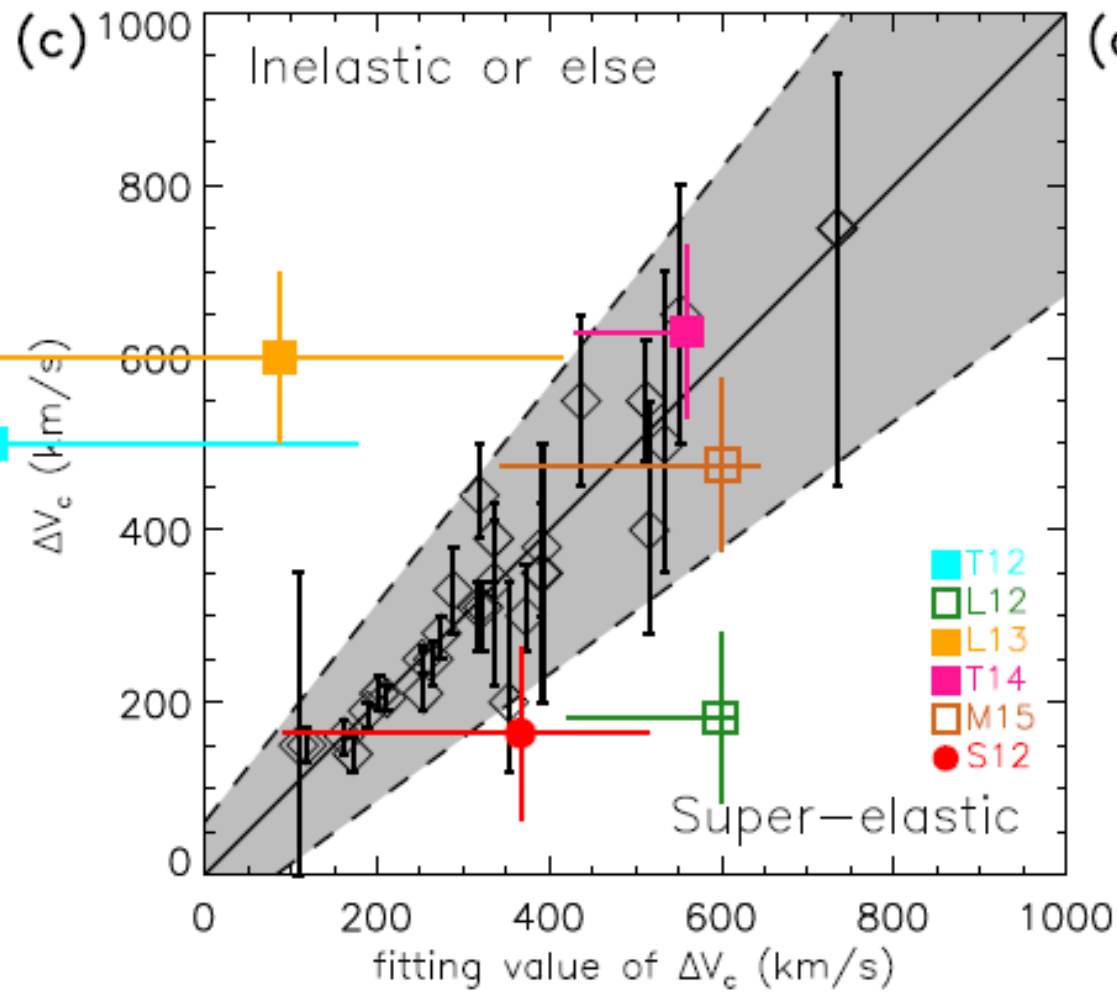
# Relationship of the approaching speed with $V_{cme1}$ and k-number



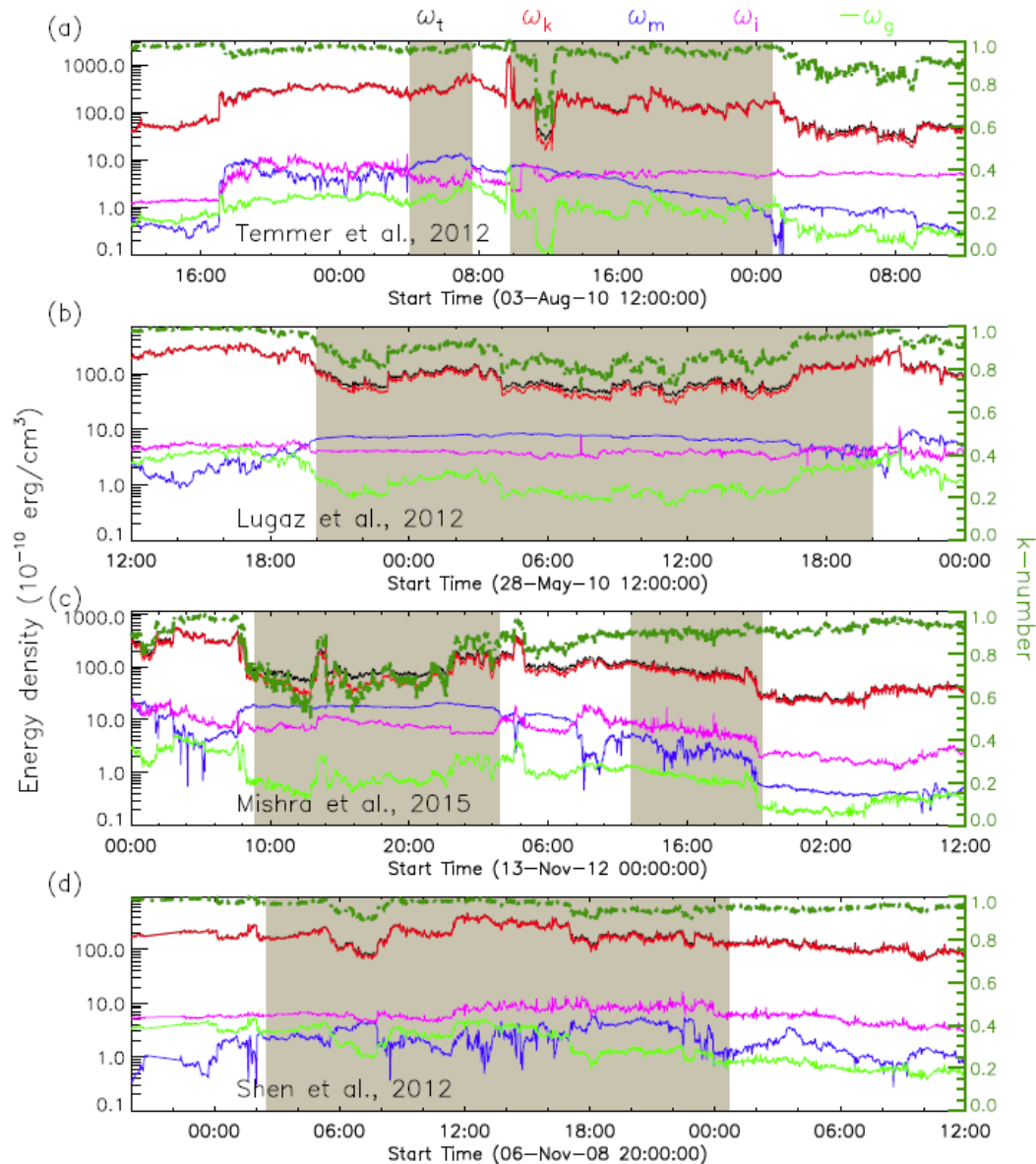
$$\Delta V_c = (0.026k - 0.013)V_{CME1}^2 - (18k - 9.2)V_{CME1} + (2360k - 1019) \quad (\text{km s}^{-1})$$

or 
$$\Delta V_c = (0.026V_{CME1}^2 - 18V_{CME1} + 2360)k - (0.013V_{CME1}^2 - 9.2V_{CME1} + 1019) \quad (\text{km s}^{-1})$$

# Diagram of the collision nature



# Derive the k-number from in-situ data



Energy density

$$\omega_k = \frac{1}{2}(m_p n_p v_p^2 + m_e n_e v_e^2)$$

$$\omega_m = \frac{B^2}{2\mu}$$

$$\omega_i = \frac{n_p k T_p + n_e k T_e}{\gamma - 1} = \frac{p_p + p_e}{\gamma - 1}$$

$$\omega_g = -\frac{GM_s}{r}(m_p n_p + m_e n_e)$$

Scaling law

$$\omega_k \propto r^{-3}$$

$$\omega_m \propto r^{-4}$$

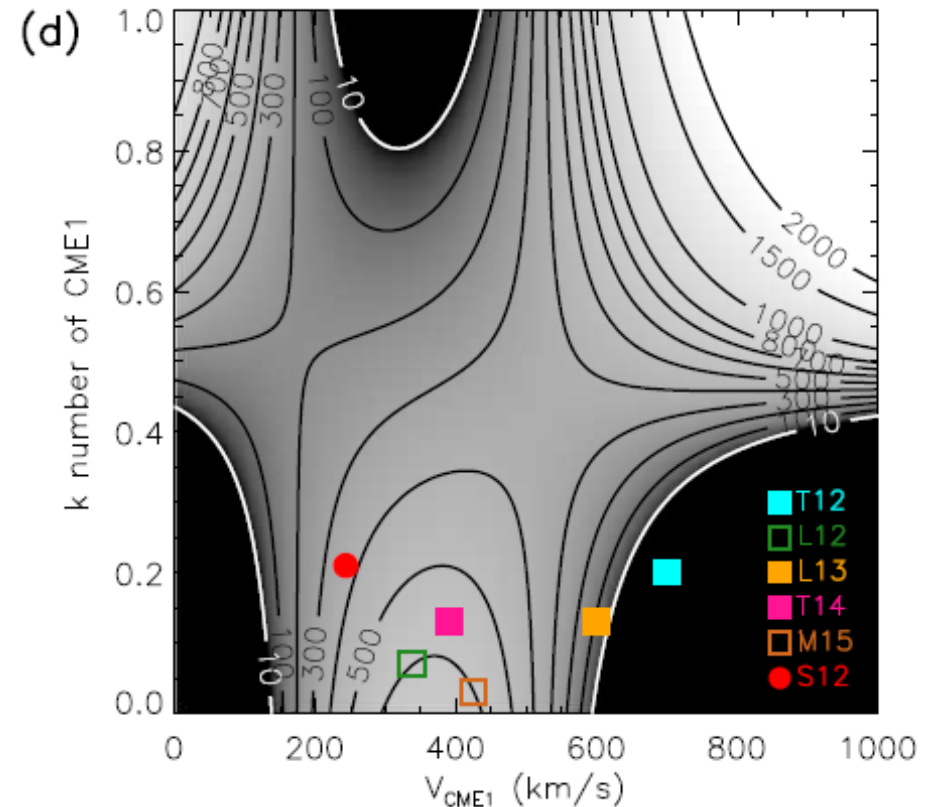
$$\omega_i \propto r^{-4}$$

$$\omega_g \propto r^{-4}$$

Average k-number of the events is 0.13

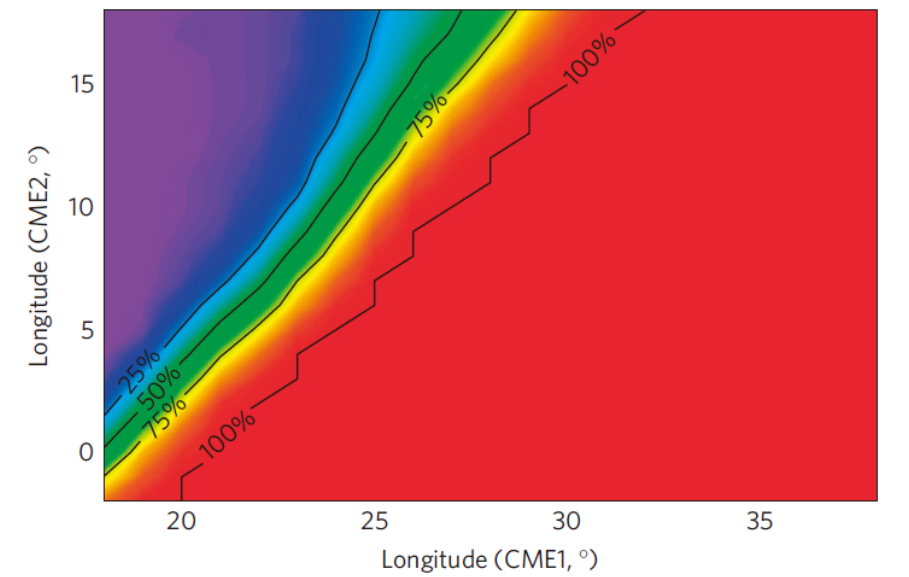
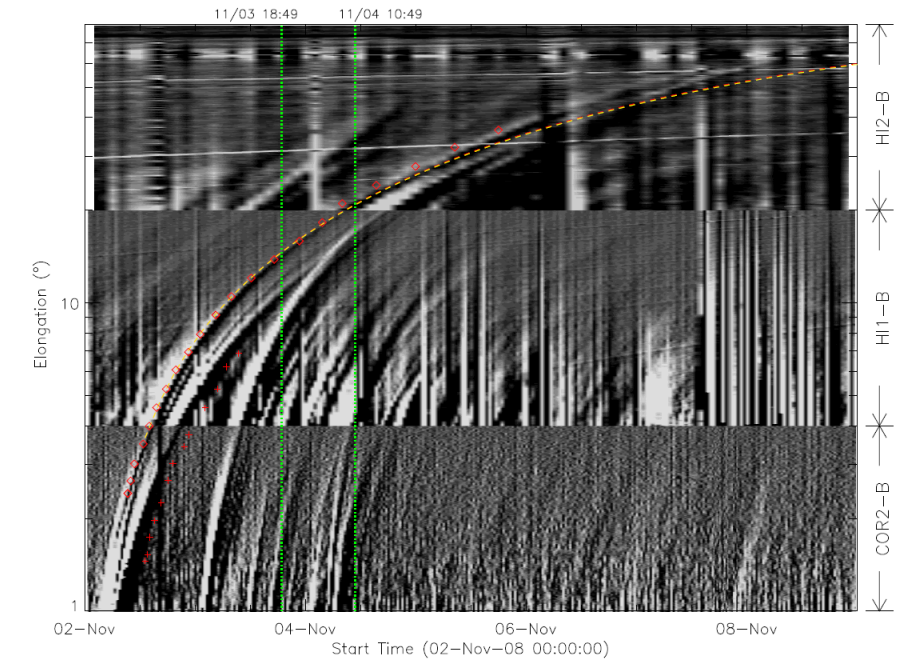
# Summary

- A smaller approaching speed is more favorable for a super-elastic collision.
- The critical approaching speed is linearly correlated with the k-number and roughly quadratically correlated with the first CME's speed.
- A diagram is inferred. It is particularly useful in roughly estimating the collision nature as long as we know the values of the CMEs' speeds and the k-number, which are all possibly obtainable from observations.
- For a super-elastic collision, the extra kinetic energy gain could be from CME's magnetic energy and/or thermal energy.



# Discussion

- Many influence factors are ignored, such as the magnetic field reconnection, shock, the approaching angle, the collision distance, background solar wind, CME mass change, etc.
  - The solar wind efficiency in acceleration CME is about 6.5% of the collision efficiency
  - Mass ratio of the two CMEs is **not** sensitive to the collision nature
  - The approaching angle does influence the results significantly --- **simple 1D collision model is not appropriate**
  - Expansion speed may also influence the results significantly --- **a model of expanding elastic balls in 3D is more appropriate**



Thanks for your attention!



# Test the effects of background solar wind

