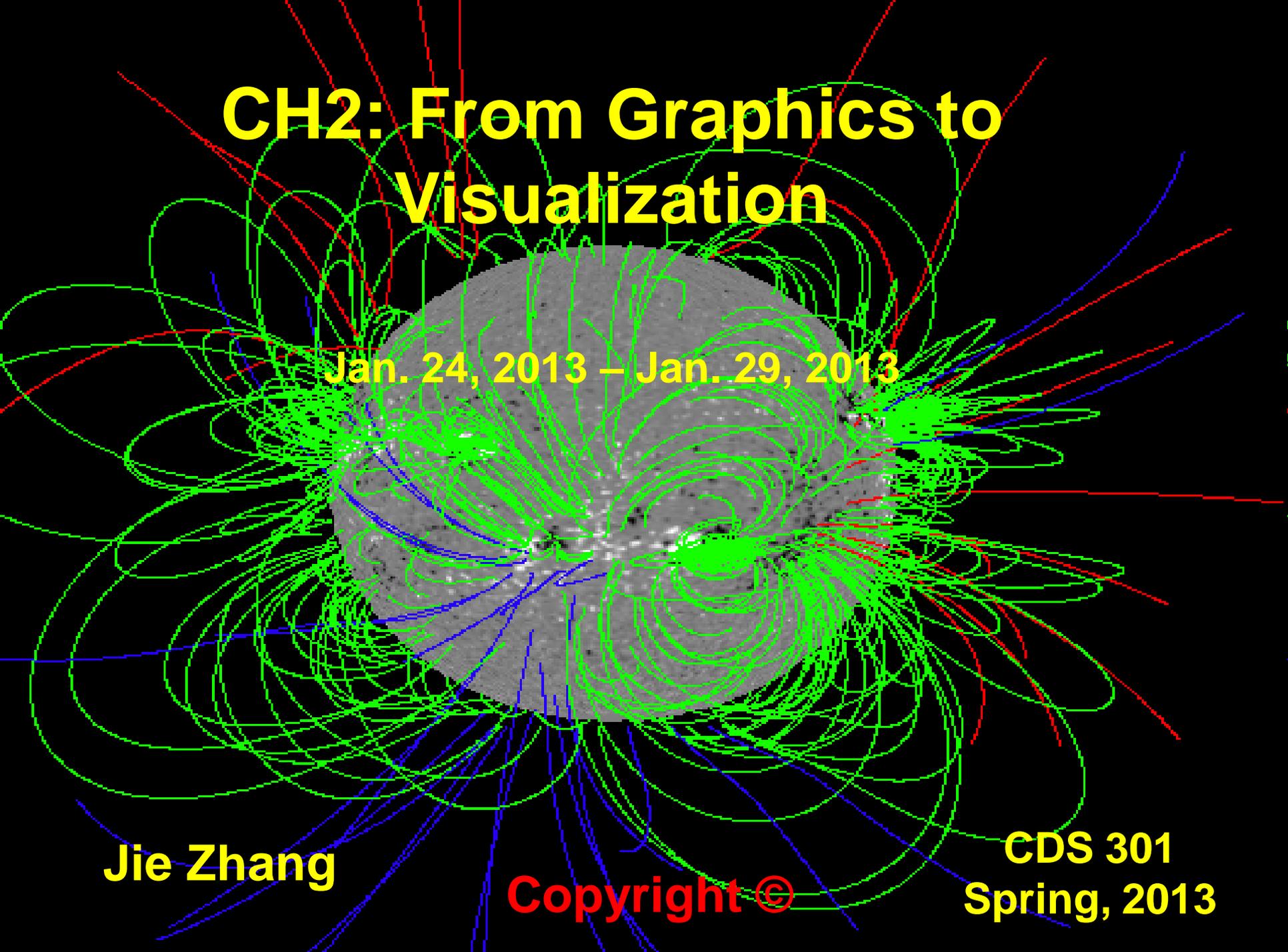


CH2: From Graphics to Visualization



Jan. 24, 2013 – Jan. 29, 2013

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CDS 301
Spring, 2013

Outline

- **Example: make a 2-D Gaussian plot**
- **Data sampling**
- **Graphic Rendering**
 - **Light Rendering Model**
- **Texture Mapping**
- **Transparency and Blending**
- **Visualization Pipeline**

2-D Gaussian Function

$$f(x, y) = e^{-(x^2 + y^2)}$$

where

$$X = [-1, 1], \quad Y = [-1, 1]$$

$$D = [-1, 1] \times [-1, 1]$$

**Compact Domain,
Continuous Data**

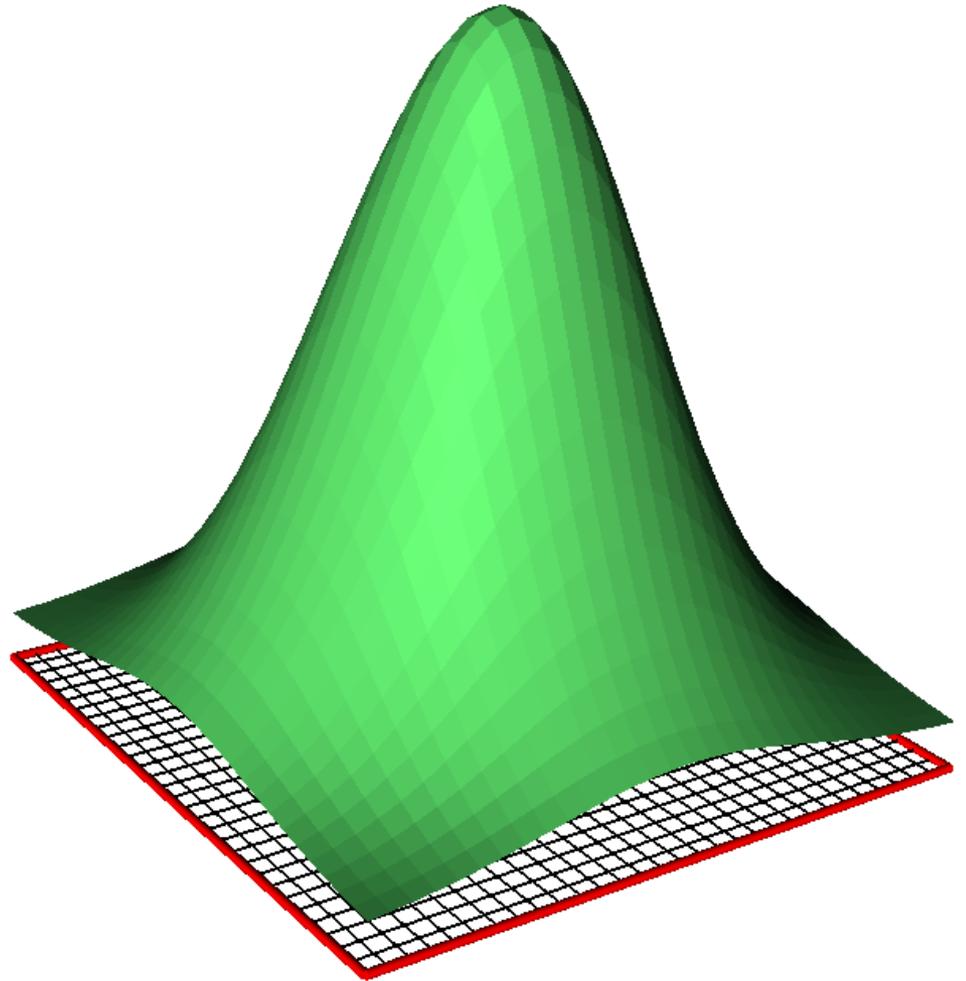
$$S \in \mathbb{R}^3$$

**A Continuous 3D Surface
in 3-D Space**

2-D Gaussian Function

Sampling:

- $N_x=30$
 - $N_y=30$
 - Uniform grid in the domain space
-
- Mapping the 3-D surface to
 - A set of four-vertex polygons, or quadrilateral



2-D Gaussian Function

Quadrilateral (**quad**) in 3-D space:

V1: (x, y, f(x,y))

V2: (x+dx, y, f(x+dx,y))

V3: (x+dx, y+dy, f(x+dx,y+dy))

V4: (x, y+dy, f(x,y+dy))

These graphic primitives are rendered fast by computers

A **quad** has uniform illumination or lighting on its surface, so called **flat shading**

2-D Gaussian Function

Implementation:

```
float X_min, X_max;
float Y_min, Y_max;
int   N_x,N_y;
float dx = (X_max-X_min)/N_x;
float dy = (Y_max-Y_min)/N_y;
float f(float,float);

for (float x=X_min;x<=X_max-dy;x+=dx)
  for (float y=Y_min;y<=Y_max-dy;y+=dy)
  {
    Quad, q;
    q.addPoint (x,y, f(x,y));
    q.addPoint (x+dx,y, f(x+dx,y));
    q.addPoint (x+dx,y+dy, f(x+dx,y+dy));
    q.addPoint (x,y+dy, f(x,y+dy));
  }
```

Rendering: the basics

- **Computer graphic rendering** generate a computer image of **3D scene**, for a given dataset

- **Ingredients:**

- A 3D scene
- A set of Lights
- A viewpoint

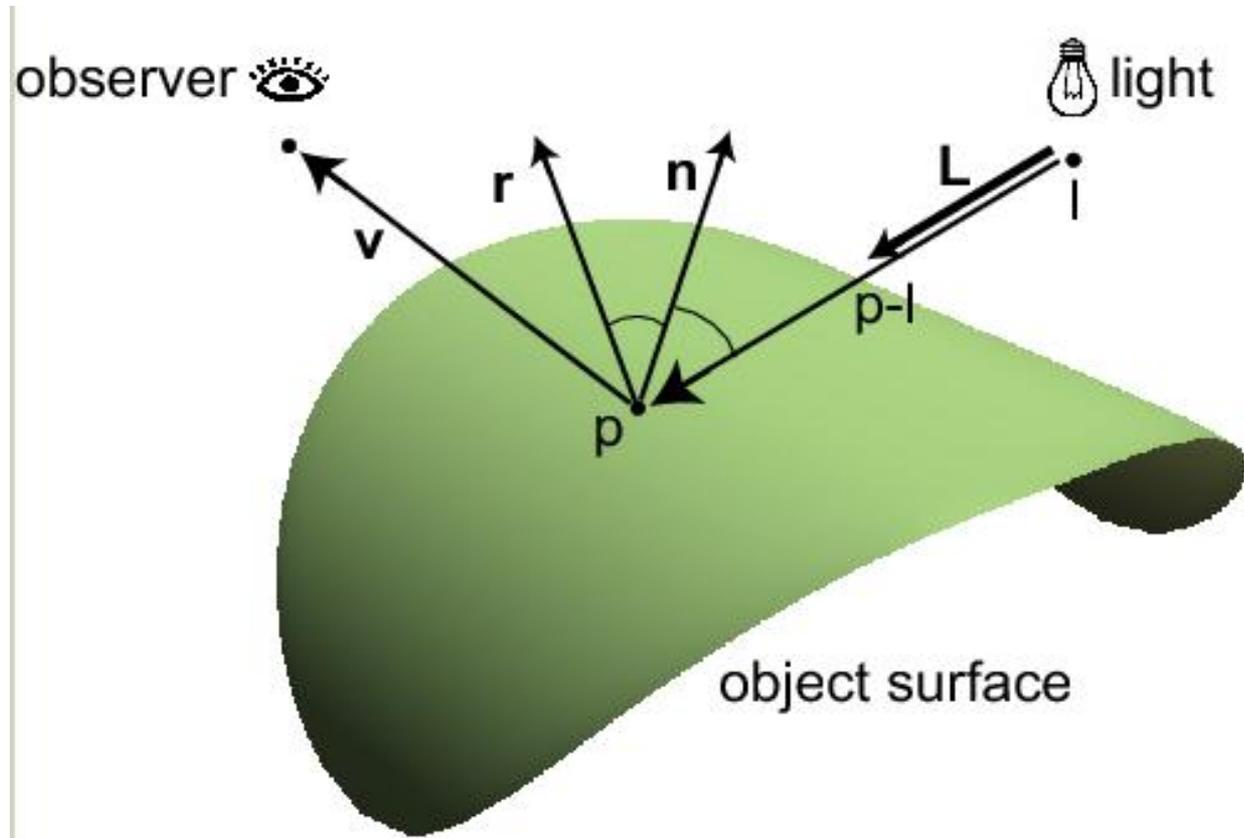
- How to determine the illumination of the primitive shapes in the 3-D scene?

Rendering Equations

- **Rendering methods differ in approximating lighting effects**
 - **Global illumination: ray tracing, accurate but computationally expensive**
 - **Local illumination: relate the illumination of a given scene point directly to the light set, not to any other scene points**
- **Phong Local Lighting Model (OpenGL)**
 - **Assuming that the scene consists of opaque objects in void space, illuminated by a point-like light source**

Phong Local Lighting Model

$$I(p, \mathbf{v}, \mathbf{L}) = I_l (C_{amb} + C_{diff} \max(-\mathbf{L} \cdot \mathbf{n}, 0) + C_{spec} \max(-\mathbf{r} \cdot \mathbf{V}, 0)^\alpha)$$



Calculate Normal Direction

Using gradient:

$$\vec{n} = \left(-\frac{\partial f}{\partial x}, -\frac{\partial f}{\partial y}, 1 \right)$$

Using normal averaging:

$$\vec{n}_i = \frac{\sum_{p_j} \vec{n}(p_j)}{N}$$

Calculate reflection Direction

$$\vec{r} = \vec{L} - 2 (\vec{L} \cdot \vec{n}) \vec{n}$$

Phong Local Lighting Model

$$I(p, \mathbf{v}, \mathbf{L}) = I_l (C_{amb} + C_{diff} \max(-\mathbf{L} \cdot \mathbf{n}, 0) + C_{spec} \max(-\mathbf{r} \cdot \mathbf{V}, 0)^\alpha)$$

$I(p, \mathbf{v}, \mathbf{L})$: intensity of the scene point

I_l : Intensity of the light

p : location of the scene point

\mathbf{V} : direction vector from p to the viewpoint

\mathbf{L} : direction vector from the light to p

\mathbf{n} : surface normal at p

\mathbf{r} : direction of the reflecting light

α : specular power α

Three coefficients:

1. C_{amb} : ambient lighting, overall effect of other objects, assuming to be constant
2. C_{diff} : diffuse lighting, scattering of the surface, equal in all direction; plastic surface
3. C_{spec} : specular lighting, mirror-like surface

Primitive Shape Shading

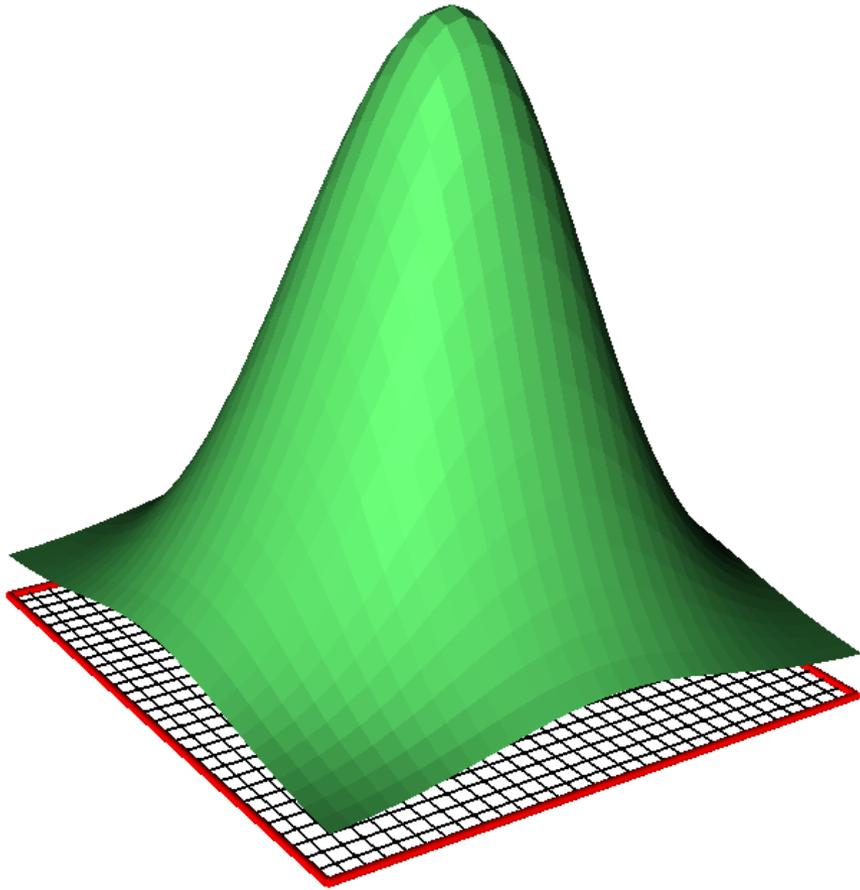
- **Flat shading:**

- **Given a polygon surface (e.g., quadrilateral), flat shading applies the lightening model once for the complete polygon, e.g., for the center point**
- **The whole polygon surface has the same light intensity**
- **The least expensive**
- **But visual artifact of the “faceted” surface**

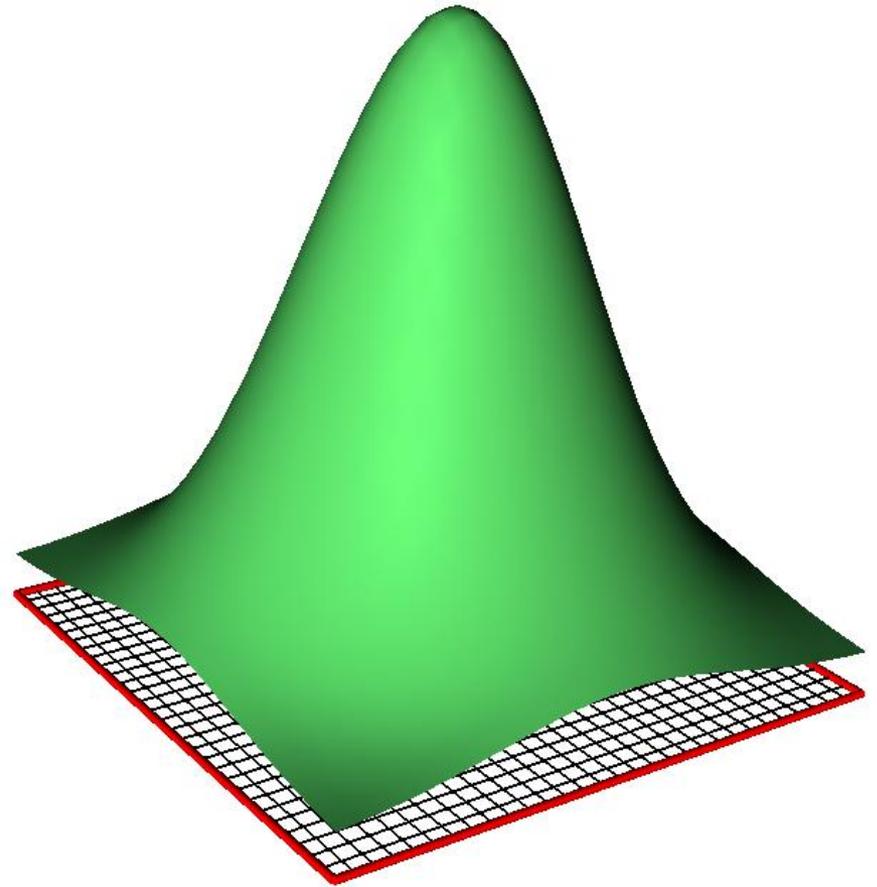
- **Gouraud shading (or smooth shading):**

- **Apply lightening model at every vertex of the polygon**
- **The intensity between the vertices are calculated using interpolation, thus yielding smooth variation**

Primitive Shape Shading



Flat Shading



Gouraud Shading

Primitive Shape Shading

Implementation:

```
-----  
glShadingMode(GL_FLAT);  
  
glColor3f(r,g,b) ;set material color  
  
glEnable(GL_LIGHTENING);  
  
glEnable(GL_LIGHT0);  
  
glLightfv(GL_LIGHT0,GL_POSITION,p);  
  
glLightfv(GL_LightT0,GL_AMBIENT,I);
```

Jan. 29, 2013

Review

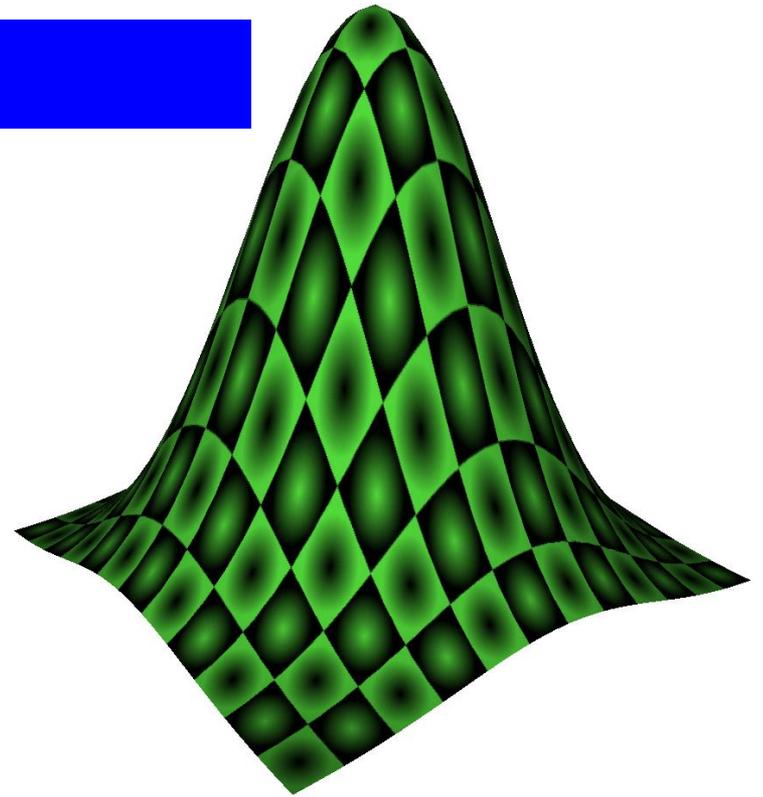
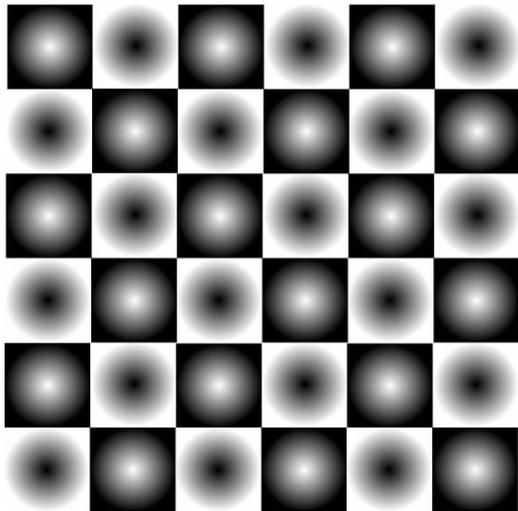
- **Example: make a 2-D Gaussian plot**
- **Sampling**
- **Mapping**
- **Graphic Rendering**
 - **Light Rendering Model**

**Then, finish up CH2
And move to CH3**

Texture Mapping

- Effectively simulate a wide range of appearance on the surface of a rendered object
- Improve the realism of visualization
- Method: pre-define a texture image, mapping the polygon vertex coordinates to texture coordinates, and then combine the texture color with the polygon color

A rendering trick

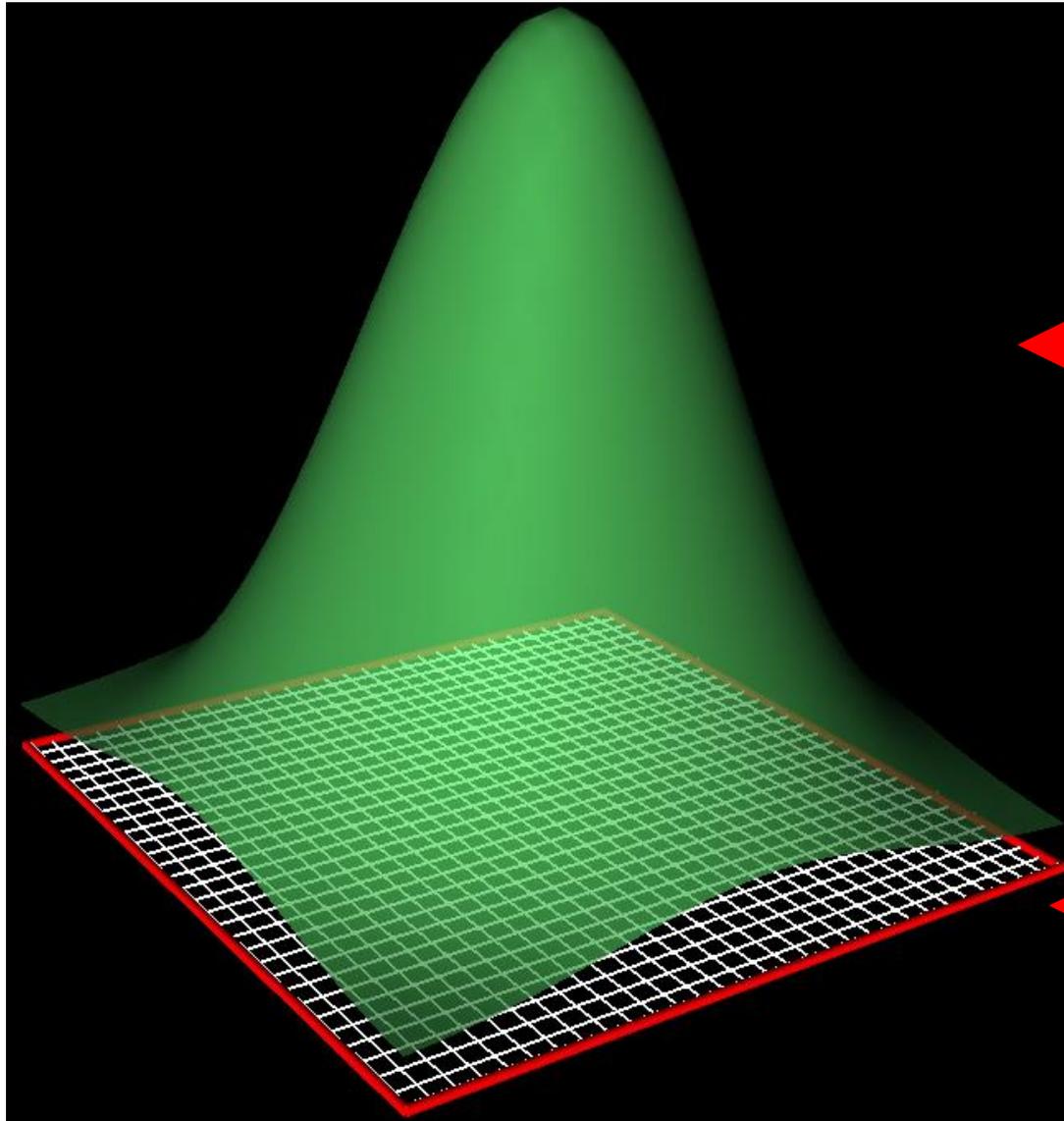


Transparency and Blending

- Rendering translucent (or half-transparent) shape
- See multiple shapes at the same time
 - e.g., the Gaussian surface and the underlying gridded domain
- Blending method (rendering the transparent effect)
 - Source: the shape is being drawn
 - Destination: the frame buffer (currently displayed image)
 - Source + Destination

Another rendering trick

Transparency and Blending



The Gaussian Surface

The Grid

Transparency and Blending

$$dst' = sf * source + df * destination$$

- The blending output is a weighted combination of the source and the destination
 - sf: source weight factor, [0,1]
 - Also called alpha component
 - df: destination weight factor, [0,1]
 - sf and df: also called blending factors

```
glBlendFunc(GL_SOURCE_ALPHA, GL_ONE);  
glColor4f(r,g,b,sf)
```

Visualization Pipeline

Input/
Output

Processes

$$f(x, y) = e^{-(x^2 + y^2)}$$

Continuous data

Data Acquisition

float data[N_x, N_y]

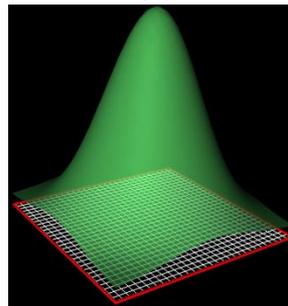
Discrete dataset

Data Mapping

Class Quad

Geometric object:
The fixed 3-D scene

Rendering



Displayed image

End