

Lect. 21, Apr. 20, 2010

①

Part 5: Electromagnetic Character of Light

polarization (CH 22)

Double Refraction (CH 22)

Maxwell's Equation (CH 23)

plain waves in a Dielectric (CH 23)

Poynting flux (CH 23)

Reflection and Refraction of EM waves (CH 24)

Polarization (CH 22)

The general wave function, also called displacement function, for 1-D (along z axis), plane wave is

$$\Psi = a \cos(kz - \omega t + \phi_0)$$

k : wave number

ω : angular frequency

ϕ_0 : initial phase

$(kz - \omega t + \phi_0)$: phase term

$v = \frac{\omega}{k}$: phase velocity

a : amplitude.

* For a plane wave: $a(x, y, z) = \text{const}$

* For multiple waves: interference and diffraction

$a(x, y, z)$ is a function of location,
 \Rightarrow fringe pattern

* Polarization: $|a(x, y, z)| = \text{const}$, constant amplitude

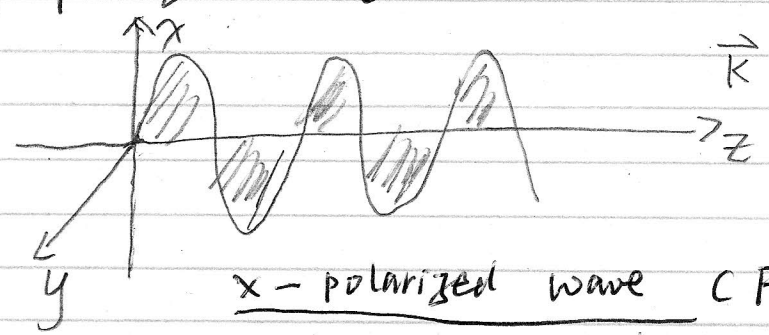
still a plane wave.

However, the direction of displacement matters

$$a \rightarrow \vec{a} = \hat{i} a_x + \hat{j} a_y$$

Polarization (CH 22) (continued)

* Linearly polarized wave



$$x(z, t) = a \cos(kz - \omega t + \phi_0)$$

$$y(z, t) = 0$$

Linear: oscillation for a given particle at z moves along a straight line

→ Also called "plane polarized" wave: oscillation of all particles contain in the same plane

→ Y-polarized wave (see Fig 22.1 b)

$$x(z, t) = 0$$

$$y(z, t) = a \cos(kz - \omega t + \phi_0)$$

→ Circularly-polarized wave (see Fig 22.1 c)

the particle moves along a circular path

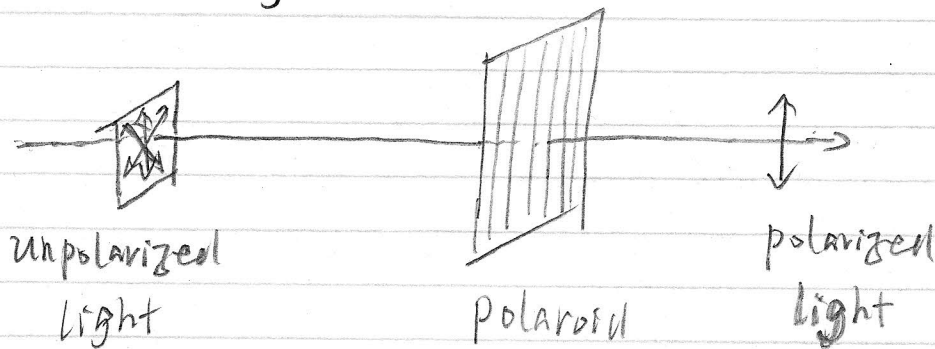
$$x(z, t) = a \cos(kz - \omega t + \phi_0)$$

$$y(z, t) = a \sin(kz - \omega t + \phi_0) = a \cos(kz - \omega t + \phi_0 - \frac{\pi}{2})$$

total amplitude $\sqrt{x^2 + y^2} = a : a \text{ constant}$

Polaroid:

only light along the pass axis is transmitted.
other lights are absorbed



(see Fig. 22.6)

Production of Polarized Light

* Wire - Grid polarizer: (see Fig. 22.8)

Electric field along the direction of wires dissipated

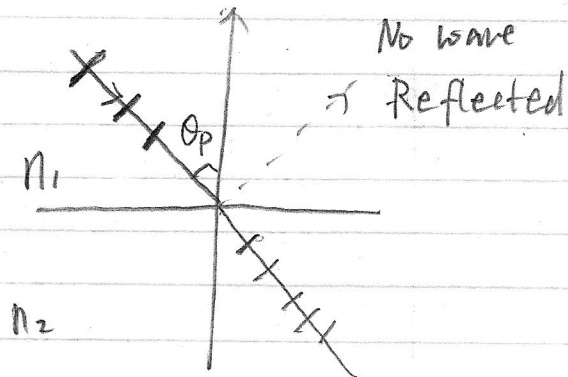
Polaroid: long chain polymer molecules that contain atoms which provide high conductivity along the length of the chain

Reflection

Incidence angle θ_p

$$\theta_p = \tan^{-1} \left(\frac{n_2}{n_1} \right)$$

Polarization angle or Brewster angle



$r_{\perp} = 0$ for the light

$$r_{\parallel} = 0$$

whose electric vector lies in the plane of incidence

* plane of incidence: incident light k + normal of surface

At $\theta = \theta_p$, \rightarrow reflected light is linearly polarized, whose $\vec{E} \perp$ plane-of-incidence

Malus' Law (CH 22.3)

$$I = I_0 \cos^2 \theta \quad (\text{see Fig. 22.15}) \quad \text{--- (1)}$$

θ = the angle between the polarization direction of the incident light and the pass axis of the polaroid.

$\theta = 0^\circ$, complete transmission

$\theta = 90^\circ$, complete block

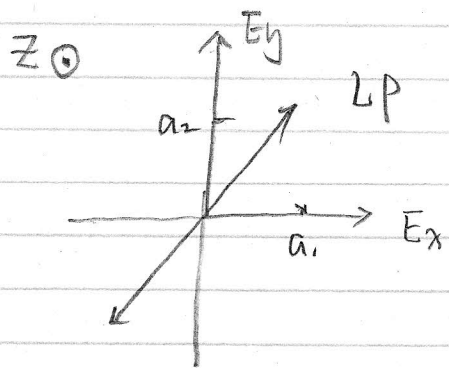
State of polarization and superposition (CH 22.4)

Consider the superposition of two linearly polarized waves both propagate along the z direction

$$\vec{E}_1 = \hat{x} a_1 \cos(kz - \omega t + \theta_1) \quad ; \quad \text{LP (linear polarized)}$$

$$\vec{E}_2 = \hat{y} a_2 \cos(kz - \omega t + \theta_2) \quad ; \quad \text{LP}$$

$$\theta = \theta_2 - \theta_1$$



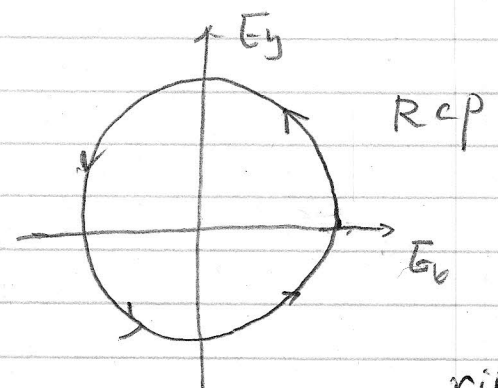
$\theta = 0 \Rightarrow \text{LP}$

or $\theta = 2\pi \cdot m$

$$\begin{cases} E_x = a_1 \cos \omega t \\ E_y = a_2 \cos \omega t \end{cases}$$

[without loss of generality,

$$z=0, \theta_1=0 \Rightarrow E_y = a_2 \cos(\omega t - \theta)$$



$\theta = \frac{\pi}{2} \Rightarrow \text{RCP: right circularly polarized}$

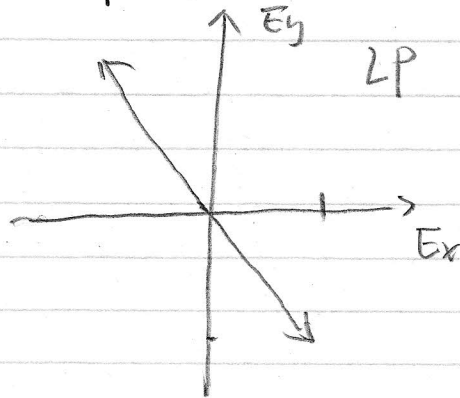
or $\theta = \frac{\pi}{2} + 2\pi \cdot m$

$$\begin{cases} E_x = a_1 \cos \omega t \\ E_y = a_2 \cos(\omega t - \frac{\pi}{2}) = a_2 \sin \omega t \end{cases}$$

$a_1 = a_2$: circular
 $a_1 \neq a_2$: elliptical

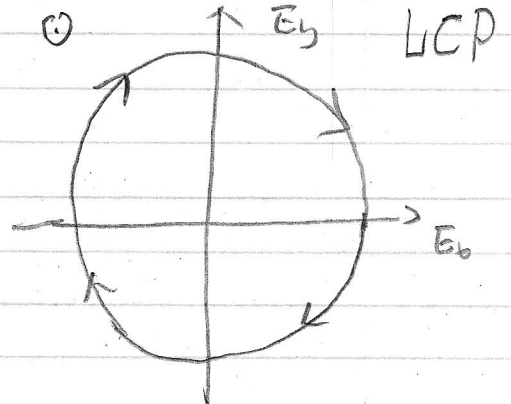
(5)

State of polarization (CH 22.4) (continued)



$$\theta = \pi \Rightarrow \text{LP}$$

$$\begin{cases} E_x = a_1 \cos \omega t \\ E_y = -a_2 \sin \omega t \end{cases}$$



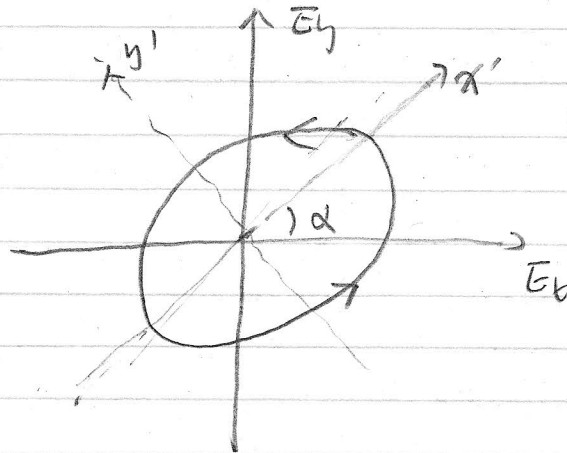
$$\theta = \frac{3}{2}\pi \Rightarrow \text{LCP}$$

$$\begin{cases} E_x = a_1 \cos \omega t \\ E_y = -a_2 \sin \omega t = a_2 \cos(\omega t - \frac{3}{2}\pi) \end{cases}$$

clock-wise rotation

If $\theta \neq 0, \frac{\pi}{2}, \pi, \frac{3\pi}{2}$ \Rightarrow EP (elliptical polarization)

LP RCP LP LCP



EP.
(x', y'), new principle axis

$$\theta = \frac{\pi}{3} \Rightarrow \text{EP}$$

$$\begin{cases} E_x = a_1 \cos \omega t \\ E_y = a_2 \cos(\omega t - \frac{\pi}{3}) \end{cases}$$

$$\tan 2\alpha = \frac{2a_1 a_2 \cos \theta}{a_1^2 - a_2^2}$$

If $a_1 = a_2$, $\tan 2\alpha \rightarrow \infty$, $2\alpha = \frac{\pi}{2} \Rightarrow \alpha = \frac{\pi}{4}$