

PHYS 306 Spring 2010
Wave Motion and Electromagnetic Radiation

Test 2

April 15, 2010

There are five questions. You need to answer four of them. You must indicate which one of the five you omit.

1. Standing waves are formed on a stretched string under tension of 10^6 dyn. The mass per unit length of the string is 0.1 g/cm. The length of the string is 50 cm. If it vibrates with five loops,

- (1) What is the wavelength of the standing wave?
- (2) What is the wave velocity along the string?
- (3) What is the angular frequency of the vibration?

2. In Young's double-hole experiment, the distance between the two holes is 1.0 mm, $\lambda = 5 \times 10^{-5}$ cm, and $D = 100$ cm.

- (1) What will be the fringe width?
- (2) Calculate I/I_{\max} where I represents the intensity at a point where the path difference is $\lambda/5$?

3. (1) Consider a nonreflecting film of refractive index 1.60. Assuming that its thickness is 8×10^{-6} cm. Calculate the wavelength (in the visible region) for which the film will be nonreflecting?

(2) In the Michelson interferometer arrangement, if one of the mirrors is moved by a distance 0.06 mm, 200 fringes cross the field of view. Calculate the wavelength?

4. For a scanning Fabry-Perot Interferometer, the transmitted interference pattern is described as, for a normal incidence,

$$T = \frac{1}{1 + F \sin^2 \frac{\delta}{2}}; \quad \delta = \frac{4\pi h}{\lambda_0}$$

- (1) For what δ_m , the transmittivity T equals 1?
- (2) Show that

$$\Delta \delta = \frac{4}{\sqrt{F}}$$

in which, $\Delta \delta$ represents the FWHM of the transmittivity; in other words, $T=1/2$ at $\delta = \delta_m + \Delta \delta / 2$

- (3) Show that the spectrum resolution

$$|\Delta \lambda_0| = \frac{\lambda_0^2}{\pi h \sqrt{F}}$$

5. A convex lens of focal length 50 cm is placed after a slit of width 0.6 mm. If a plane wave of wavelength 6000 Å falls normally on the slit, calculate the separation between the first minima on either side of the central maximum.